Mathematical transmission models are useful tools for predicting the magnitude, duration, and severity of the severe acute respiratory coronavirus 2 (SARS-CoV-2) pandemic. However, widely used national-level models might not capture regional heterogeneity. The coronavirus disease (COVID-19) outbreak in Colorado, USA, has been the subject of numerous discrepant projections from the Institute for Health Metrics and Evaluation and other modeling groups (1), which might have structural and data source explanations, highlighting the need for ensuring that models are fit to local epidemiologic data (2–4).

We report on our experience using a locally tailored model to inform policy in Colorado. Social distancing policies, intended to decrease contact rates, have been cornerstone public health tools for pandemic control, and these strategies have been adopted to control SARS-CoV-2 globally (2,5). Until recently, evidence of the effects of social distancing has come primarily from studies of the consequences of school and transit closures on influenza transmission (3,4,6). Early evidence suggests that social distancing policies can suppress transmission of SARS-CoV-2 (7,8), and recent evidence suggests a strong correlation between mobility and transmission reduction (9). However, these studies largely focused on periods when social distancing policies were in place, leaving critical questions unanswered regarding how long populations will comply with such measures and what happens when policies are relaxed.

One of the defining characteristics of the COVID-19 pandemic is the need for rapid response in the face of imperfect and incomplete information. Mathematical models of infectious disease transmission can be used in real-time to estimate parameters, such as the effective re-

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productive number ($R_e$) and the efficacy of current and future intervention measures, providing time-sensitive data to policy-makers (10). We describe development of such a model, in close collaboration with the Colorado Department of Health and Environment and the Governor’s office, to gauge the current and future effects of early policies to decrease social contacts and, later, the gradual relaxing of stay-at-home orders.

We developed a compartmental susceptible-exposed-infected-recovered (SEIR) model calibrated to statewide COVID-19 case and hospitalization data to estimate changes in the contact rate and the $R_e$ after emergence of SARS-CoV-2 and the implementation of statewide social distancing policies in Colorado. We supplemented model estimates with an analysis of mobility by using mobile-device location data. Estimates were generated in near real time, at multiple time-points, with a rapidly evolving understanding of SARS-CoV-2. At each time point, we generated projections of the possible course of the outbreak under future social distancing scenarios. Findings were regularly provided to key Colorado decision-makers. We present estimates generated at multiple time points to document how our model, estimates and projections evolved over time. Although our analysis is specific to Colorado, our experience highlights the need for locally calibrated transmission models to inform public health preparedness and policymaking, along with ongoing analyses of the impact of policies to slow the spread of SARS-CoV-2.

Methods

COVID-19 Timeline and Policies

The first SARS-CoV-2 case was reported in Colorado on March 5, 2020, and a rapid succession of policies to control transmission followed (Table 1). The Colorado governor formally declared a disaster emergency on March 11. During March 14–April 16, a total of 35 executive orders were mandated to curb SARS-CoV-2 transmission, including school closures, reduction in workforce percentages, and shelter-in-place (stay-at-home) orders. In conjunction with state executive orders, the Colorado Department of Health and Environment issued orders closing restaurants, bars, and other congregate environments on March 17 and prohibiting gatherings of >10 persons on March 19. A state-wide stay-at-home order was in effect during March 26–April 26. Transition to a less restrictive phase, safer-at-home, began on April 27, which enabled some businesses to reopen with restrictions. The metropolitan Denver counties, comprising >50% of the population of Colorado, were under extended stay-at-home orders until May 8.

Reported Case and Hospitalization Data

Hospitalization data are a robust indicator of transmission trends compared with reported case data because reported case data are sensitive to testing capacity. However, because COVID-19 hospitalization data were sparse early in the epidemic, we initially fit models to reported COVID-19 cases from the Colorado Electronic Disease Reporting System (CEDRS). We fit models to the daily number of symptom onsets to reflect a biologically meaningful process (report date can be sensitive to testing lags). Missing onset dates were imputed as report date minus 7 days, the median onset-to-report lag. In May, we began fitting models to the daily number of hospitalized COVID-19 patients because we suspected that reported cases captured a variable proportion of infections over time because of increases in testing capacity. Daily hospital census records were obtained from EMResource (https://emresource.juvaire.com). Because EMResource appeared to underreport COVID-19 hospitalizations during March, we inferred COVID-19 hospitalizations by using CEDRS before April 8 (Appendix Figure 1, https://wwwnc.cdc.gov/EID/article/27/9/20-4167-App1.pdf).

Model Description

We used a deterministic age-structured SEIR model with 3 age groups (<30, 30–59, and ≥60 years of age) to estimate key model parameters and project the number of COVID-19 hospitalizations (Appendix). In the model, we assume a single virus introduction event occurring on January 24, a date extrapolated from the first reported cases in Colorado.

In the model, the probability that an infected person shows development of symptoms (13) and needs hospitalization or ICU care is age dependent (14) (Appendix Table 1). All persons have an equal probability of exposure and infection, regardless of age. Initially, we used published estimates (15) for the proportion of symptomatic case-patients requiring hospitalization and critical care. Starting in May, with sufficient hospitalization data, we generated Colorado-specific estimates of the probability of hospitalization and critical care among case-patients by using model-fitting approaches, which enabled us to better account for underlying health status and patterns of care in Colorado (16).

The model includes 3 types of transmission-reducing parameters: social distancing, mask wearing,
Table 1. Key state-level events, executive orders, and policies directed at controlling transmission of SARS-CoV-2, Colorado, USA, 2020*

<table>
<thead>
<tr>
<th>Policy/event of COVID-19</th>
<th>First case of infection with SARS-CoV-2 reported</th>
<th>First case of infection with SARS-CoV-2 reported</th>
<th>Date announced</th>
<th>Policy effective date</th>
<th>Policy effective until</th>
</tr>
</thead>
<tbody>
<tr>
<td>First case of COVID-19</td>
<td>First case of infection with SARS-CoV-2 reported</td>
<td>First case of infection with SARS-CoV-2 reported</td>
<td>Mar 5</td>
<td>NA</td>
<td>NA</td>
</tr>
<tr>
<td>Executive Order D 2020 003</td>
<td>Disaster emergency</td>
<td>Mar 10</td>
<td>Mar 11</td>
<td>Apr 11</td>
<td></td>
</tr>
<tr>
<td>Executive Order D 2020 004</td>
<td>Ski resort closure</td>
<td>Mar 14</td>
<td>Mar 15</td>
<td>Apr 22</td>
<td></td>
</tr>
<tr>
<td>Executive Order D 2020 006</td>
<td>Extension of ski resort closure</td>
<td>Mar 18</td>
<td>Mar 18</td>
<td>Apr 17</td>
<td></td>
</tr>
<tr>
<td>CDPHE Order 20–22</td>
<td>Closure of bars, restaurants, theaters, gyms, and casinos</td>
<td>Mar 16</td>
<td>Mar 16</td>
<td>Apr 16</td>
<td></td>
</tr>
<tr>
<td>CDPHE Order 20–23</td>
<td>Prohibition of &gt;10 person gatherings</td>
<td>Mar 19</td>
<td>Mar 19</td>
<td>Apr 19</td>
<td></td>
</tr>
<tr>
<td>Executive Order D 2020 007</td>
<td>School closures during Mar 18–Apr 17</td>
<td>Mar 18</td>
<td>Mar 18</td>
<td>Apr 17</td>
<td></td>
</tr>
<tr>
<td>Executive Order D 2020 013</td>
<td>Reduction of in-person workforce by 50%</td>
<td>Mar 22</td>
<td>Mar 24</td>
<td>May 10</td>
<td></td>
</tr>
<tr>
<td>Executive Order D 2020 017</td>
<td>Stay-at-home order: directive to require all residents of Colorado to stay home unless in pursuit of essential items (i.e., food) or working for critical businesses and ordering noncritical businesses to close temporarily.</td>
<td>Mar 25</td>
<td>Mar 26</td>
<td>Apr 11</td>
<td></td>
</tr>
<tr>
<td>Executive Order D 2020 021</td>
<td>Extension to school closures until Apr 30</td>
<td>Apr 1</td>
<td>Apr 1</td>
<td>May 1</td>
<td></td>
</tr>
<tr>
<td>Executive Order D 2020 024</td>
<td>Stay-at-Home extension</td>
<td>Apr 6</td>
<td>Apr 6</td>
<td>Apr 26</td>
<td></td>
</tr>
<tr>
<td>Executive Order D 2020 039</td>
<td>Ordering workers in critical businesses and government functions to wear nonmedical face coverings</td>
<td>Apr 17</td>
<td>Apr 17</td>
<td>May 17</td>
<td></td>
</tr>
<tr>
<td>Executive Order D 2020 041</td>
<td>Suspension of school closures until end of school year</td>
<td>Apr 22</td>
<td>Apr 22</td>
<td>May 20</td>
<td></td>
</tr>
<tr>
<td>Executive Order D 2020 044</td>
<td>Safer at home: All susceptible persons and those who have COVID-19 instructed to stay at home. State residents directed to limit interactions, only travel for essential needs, and limit gatherings to ≤10 people in public and private spaces. Nonmedical mask coverings recommended. Retail businesses can open for curbside delivery, elective medical, dental, and veterinary surgeries and procedures resume. Retail businesses and personal services (e.g., salons) can open. Offices can open at 50% capacity.†</td>
<td>Apr 26</td>
<td>Apr 27–May 4</td>
<td>May 27</td>
<td></td>
</tr>
<tr>
<td>Executive Order D 2020 058</td>
<td>Disaster emergency extension</td>
<td>May 7</td>
<td>May 7</td>
<td>Jun 6</td>
<td></td>
</tr>
<tr>
<td>Executive Order D 2020 067</td>
<td>Extending EO D 2020 039, ordering workers in critical businesses and government, to wear nonmedical face coverings</td>
<td>May 16</td>
<td>May 16</td>
<td>Jun 16</td>
<td></td>
</tr>
<tr>
<td>Executive Order D 2020 079</td>
<td>Extension to EO D 2020 044: Safer at Home to permit public places to offer outdoor dining, and limited indoor dining</td>
<td>May 25</td>
<td>May 25</td>
<td>Jun 1</td>
<td></td>
</tr>
</tbody>
</table>

*COVID-19–relevant executive orders are detailed in (11) and CDPHE policies are described in (12). CDPHE, Colorado Department of Public Health and Environment; COVID-19, coronavirus disease; EO, executive order; NA, not applicable; SARS-CoV-2, severe acute respiratory syndrome coronavirus 2.
†Retail business and personal services were permitted to open on May 1, offices were permitted to open at 50% capacity on May 4. All other measures went into effect April 27.

and self-isolation of symptomatic persons. Social distancing was modeled as a reduction in the contact rate between susceptible and infectious persons by multiplying the transmission parameter, \( \beta \), by (1 - social distancing). We defined contacts as interactions that could enable spread of infections from an infected person to a susceptible person. The term social distancing is used to encompass all contact-reducing behaviors and policies, including working from home, school closures, maintaining physical distancing, socializing outdoors (vs. indoors), and increased hygiene. Social distancing was modeled in phases coinciding with major events and policy measures (Figure 1). Phase 1 (March 17–25) corresponds with mid-March policies and increasing public concern regarding COVID-19, phase 2 (March 26–April 26) corresponds with the state-wide stay-at-home order, phase 3 (April 27–May 8) is the period when half the state transitioned to safer-at-home, and phase 4 (May 9–June 3) is the period when safer-at-home was in effect statewide.

We added mask wearing to the model in May (fits 3 and 4) in response to increasing evidence that masks are effective for controlling transmission (17,18). We modeled the effect of mask wearing as a reduction in the spread of infections from asymptomatic and presymptomatic persons to nonhousehold contacts. More recent evidence suggests that masks might also protect the wearer, an added benefit not considered here (19). The effectiveness of mask wearing depends on the ability of the mask to trap infectious particles and the proportion of the population...
wearing masks. We assume in the model that masks made from household materials are ≈50% effective in trapping infectious particles when worn properly (17,18). Previous studies estimated that ≈23% of contacts occur at home (20). Because persons spent more time at home during the pandemic, we assumed that 67% of the contact of an individual is with nonhousehold members. We assumed that mask wearing was uniform across asymptomatic and presymptomatic persons and fit the proportion of the population wearing masks beginning on April 4, the date of the governor’s press conference advising persons living in Colorado to wear masks. Because some transmission might also occur by fomites, we modeled mask effectiveness as a net 27% reduction in infectiousness among asymptomatic persons wearing masks. In addition, we assume mask wearing decreases transmission by presymptomatic persons (21,22); this is modeled as a 3.4% reduction in infectiousness for symptomatic persons wearing masks (assuming that symptomatic persons are asymptomatic on 1 of 8 infectious days). This model does not account for potential reduction in infectiousness by symptomatic persons who are assumed to isolate (23).

We modeled self-isolation assuming that a proportion of symptomatic case-patients self-isolate 24 hours after the onset of symptoms, and that self-isolation reduces transmission by symptomatic persons to non-household contacts. This assumption is modeled as a 59% reduction in contacts by symptomatic persons who self-isolate. Self-isolation begins in the model on March 5 and the proportion of symptomatic persons who self-isolate is fit to the data.

**Estimating Social Distancing and Other Transmission-Reducing Interventions**

We inferred the effect of social distancing and other interventions on transmission by using an algorithm-based optimization procedure at 4 different time points from April through June. We used the same approaches to estimate parameters that might vary regionally or for which there was considerable uncertainty in the literature (Table 2). We identified best-fitting parameter values by using a least-squares cost function that minimized difference between the model-estimated and observed number of reported SARS-CoV-2 cases in Colorado (fits 1 and 2) and the observed number of COVID-19 hospitalizations (fits 3 and 4). When fitting to cases (fits 1 and 2), it was necessary to also fit a parameter for the estimated probability that cases would be detected by state surveillance. We minimized the cost function by using a 2-stage fitting algorithm in R (27) and used the FME package (28) by first applying a pseudo-random optimization algorithm (29) to find a

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**Figure 1.** Emergence of COVID-19, Colorado, USA, 2020, showing policy-based responses (A) and definition of 4 distinct social distancing phases (B) corresponding with early closures (phase 1, March 17–25); statewide stay-at-home (phase 2, March 26–April 26), statewide partial transition to safer-at-home (phase 3, April 27–May 8); statewide safer-at-home (phase 4, May 9–June 3). Social distancing parameters were estimated at 4 points during March–June by using model fitting procedures and reported case data (fits 1 and 2) and hospital census data (fits 3 and 4). In light of the 5.1 day mean incubation period, the ≈7-day lag between symptom onset and case report, and the ≈8-days between symptom onset and hospitalization based on state records, there are ≈12 and 13 day lags between infection and case report, and infection and hospitalization, respectively (gray boxes). Thus, at each model fit, we could estimate social distancing parameters reflecting transmission conditions up to 12 (fits 1 and 2) or 13 (fits 3 and 4) days before the fit date. Asterisks (*) indicate estimate generated for only part of the period. COVID-19, coronavirus disease; P, phase.
region of minimum difference between the model and the data. The second phase used least-squares optimization applying the Levenberg-Marquardt algorithm (30). We calculated 95% CIs by using a Markov Chain Monte Carlo simulation with an adaptive Metropolis algorithm with 1,500 iterations (28). This method obtains 95% CIs by sampling from a Gaussian distribution around the mean trajectory of the ordinary differential equation model. By the end of March, the differential sensitivity matrix was full rank, and thus all 6 parameters were identifiable for all datasets used (Appendix Figure 3).

Because of the median 7-day lag between symptom onset and reporting, on April 3 (fit 1), we included cases that had a symptom onset date through March 26 for model fitting, which enabled us to generate a preliminary estimate of phase 1 social distancing. On April 16 (fit 2), we included cases that had an onset date through April 9 for model fitting, which enabled us to refine estimates of social distancing during phase 1 and generate preliminary estimates of social distancing during phase 2. We generated a preliminary estimate of phase 3 social distancing on May 15 (fit 3) and then re-estimated on June 16 (fit 4), when social distancing during phase 4 was estimated. We estimated the proportion of the population wearing masks in fits 3 and 4 with the effectiveness assumptions defined and estimated the effective reproduction number (R\text{e}) from the model output (Appendix). We additionally estimated the overall number of hospitalizations prevented as a result of decreasing contacts by comparing the fitted model on June 16 with a reference scenario assuming no reduction of the contact rate (social distancing = 0%).

### Projections of COVID-19 Hospitalizations and ICU Need

We used the fitted parameters to generate projections of future hospital and critical care needs under different scenarios. Changes in social distancing were implemented beginning 2 weeks after the date of model fitting to account for lags in policy implementation. All other parameters were held fixed as estimated from the model. Preparing for and meeting ICU load was a critical decision-making issue.

### Population Mobility

We used SafeGraph (https://www.safegraph.com) data to examine changes in mobility in Colorado from March through June. Specifically, we used an aggregated and anonymized measure of time away from home reported at the census block group. We calculated changes in mobility as a percent decrease in time away from home relative to pre-epidemic baseline: January 29–February 15 (mean 2.3 hours).
Impact of Policies to Reduce Spread of SARS-CoV-2

We examined the relationship between mobility and transmission by calibrating the transmission parameter, $\beta$, conditional on time away from home at baseline. We then projected the model forward, enabling the parameter for the daily time away from home to change according to observed mobility data. These projections assume no other transmission reducing behavior (i.e., no mask wearing or self-isolation) to avoid conflating parametric assumptions with changes in observed mobility, nor changes to any other aspects of the model.

Results

Estimating Efficacy of Social Distancing and Other Transmission-Reducing Interventions

On April 3 (fit 1), we generated a preliminary estimate of social distancing during phase 1, which equated to an ≈45% decrease in the contact rate (Table 2; Figure 2), and $R_e$ decreased from 5.3 to 2.4 (Figure 3). Because of the ≈12-day lag between infection and case report, this preliminary estimate was through March 21. On April 16 (fit 2), with more complete case data, the updated estimate of social distancing during phase 1 was greater: a 65% decrease in the contact rate. At this point, we generated a preliminary estimate of the level of social distancing during the first 2 weeks of phase 2 (March 26–April 4): 76%. $R_e$ was estimated to be 0.9. Incorporating increasing data and using COVID-19 hospitalizations instead of case reports, on May 15 (fit 3), we re-estimated phase 1 and phase 2 parameters, which indicated transmission reduction had been more moderate initially (social distancing = 52% for phase 1), and greater for phase 2 (social distancing = 80%). On May 15, which was 18 days after the end of the stay-at-home order, there was no evidence of an increase in hospitalizations or contact rate due to decreased restrictions, noting that because of the ≈13-day lag between infection and hospitalization, this estimate reflects transmission through May 2. A month later on June 16 (fit 4), a greater decrease in transmission was estimated for phase 3 (social distancing = 85%), and the estimated decrease in contact rates during safer-at-home (phase 4) was 90%. Estimated $R_e$ decreased to 0.6 during phase 4.

Estimated Reduction in Hospitalizations from Decreased Contacts

As of June 16, a total of 5,272 COVID-19 hospitalizations in Colorado had been reported to CEDRS, and EMResource data strongly suggested under-reporting of COVID-19 hospitalizations to CEDRS during April and May. Using CEDRS and EMResource data, we found that the SEIR model estimated a cumulative of 5,344 COVID-19 hospitalizations in Colorado by Jun 16 (Figure 2, panel D).

Figure 2. Observed (black bars) versus model-estimated (green line) number of reported coronavirus disease cases (panels A, B) and hospitalizations (panels C, D), Colorado, USA, 2020, based on models calibrated at 4 points in the early months of the epidemic. Model-based estimates were generated by using an age-structured susceptible-exposed-infected-recovered model, and best-fit parameter values were estimated based on observed data shown. Reported cases are shown by using symptom onset date or report date minus 7 days if onset date was missing, in accordance with onset to report lags for Colorado during this period.
Assuming that no measures had been taken to alter individual behavior or risk perception (social distancing 0% throughout), we estimate that >173,000 hospitalizations would have occurred by that same date, suggesting that ≈97% of potential hospitalizations were avoided as a result of decreases in effective contacts.

Projecting Hospitalizations and ICU Need
We provide projected hospitalizations (Figure 4) and ICU need (Figure 5) that were generated from each of the 4 model fits. Fit 1, produced with the least available data, substantially overestimated hospitalizations and ICU need compared with later fits and predicted that ICU capacity would be exceeded even if 80% contact reduction was achieved. As data accumulated and transmission slowed in the state, the estimated peaks under all possible levels of social distancing decreased and shifted later in the year, and projections indicated contact reduction would need to remain at or above ≈70% to prevent exceeding ICU capacity.

Association between Changes in Mobility and Contact Rates
Residents of Colorado decreased activity outside the home starting in early March (Figure 6, panel A). The trends in mobility data suggest that, on average, the time spent away from home decreased by ≈60% from February to mid-April. Time away from home began to increase in late April, before the end of statewide stay-at-home orders, and increased steadily through June. Mobility metrics initially reinforced estimated social distancing levels, and percent reduction in time away from home coincided with estimated transmission reduction resulting from social distancing (Figure 6, panel B). However, increased time away from home in late April contrasted with estimated infectious contact reduction, which remained high through June. We compared hospitalizations simulated from mobility data to observed and observed a relatively strong association up until late April (Figure 6, panel C). After that, the modeled and observed trends decoupled, indicating that other behaviors or interventions not captured by mobility played a major role in transmission reduction.

Discussion
We used an SEIR transmission model, calibrated to local COVID-19 case and hospital data, to estimate the collective impact of individual behaviors and public policy measures in reducing COVID-19 transmission in Colorado during 2020, providing time-sensitive estimates of the pandemic trajectory to policy-makers to assist in decision-making. COVID-19 policies introduced during March and April were followed by substantial decreases in contact rates and suppression of the $R_e$ well below 1, in agreement with other
studies of nonpharmaceutical interventions to decrease SARS-CoV2 transmission (31–34). These values remained low after the stay-at-home order was lifted and mobility increased.

The continued suppression of transmission might be explained, in part, by transmission control policies that remained in effect and/or were implemented after stay-at-home ended: outbreak prevention and control strategies in long-term care facilities persisted, capacity limits were implemented for businesses and restaurants, and mass gatherings were banned. Moreover, the state reopened slowly during April and May. Given the typical lags between infection and hospitalization, the estimates do not capture the impact of reopening measures implemented during or after late May (e.g., restaurant openings).

Mobility, assessed by using mobile-device data, generally reflected state-level policy during March–June but mirrored transmission only in the early months of the pandemic. Mobility decreased rapidly in March in concert with early transmission control policies and the statewide stay-at-home order, and mobility increased as social distancing policies were relaxed. Consistent with our findings, others have found that US population mobility was reactive to policy during March: greater perceived disease prevalence and governmental stay-at-home orders resulted in less mobility and social interaction (35–37). However, in Colorado, lifting stay-at-home orders and concurrent increases in mobility do not appear to have led to increased transmission, indicating the limitations in using mobility data to predict transmission. These results warrant further investigation in other contexts to help clarify the utility of mobility data in SARS-CoV-2 forecasting, particularly during reopening phases.

Mobility data can be used to estimate when and where persons are congregating, a precondition for transmission, but do not sufficiently capture behaviors such as mask wearing, physical distancing, or moving activities outside. Those individual behaviors can play a critical role in spreading infections, and understanding what drives those behaviors can improve epidemic response. Public perception of and reaction to perceived risk is multifactorial, and, although clearly influenced by policy, in a time of heightened fear, local policy probably plays only a partial role in determining risk-reducing behavior. Rapid and frequent introduction of COVID-19-related policy measures and public communication by government officials at the national, state, and local scales probably increased fear and public risk perception regarding COVID-19 transmission, and contributed to adoption of transmission-reducing behaviors before the start of and beyond the end of stay-at-home orders (38). Conversely, persons might perceive decreased risks and abandon risk-reducing behaviors when transmission control policies are relaxed, a

Figure 4. Projected coronavirus disease hospitalizations, Colorado, USA, 2020. If current trajectory continued (black line) and for a range of social distancing scenarios (colored lines) generated by models calibrated at 4 time points during April–June (fit 1: Apr 3; fit 2: April 16; fit 3: May 15; fit 4: June 16). Current trajectory was based on estimated parameters generated for each fit. Social distancing is modeled as a percent reduction in the contact rate (from baseline), and changes in social distancing are introduced 2 weeks after model fitting date. All other fitted parameters are held at the estimated values for each fit. Because peak hospitalization estimates from fit 1 were substantially higher than estimated for later fits, the y-axis is scaled to 50,000 as opposed to 25,000 for fits 2–4. Numbers in parentheses are current values.
phenomenon we suspect contributed to an increase in COVID-19 transmission in Colorado during July 2020 (39). Research on how risk perception and behavior fluctuates in relationship to the epidemic trajectory can improve communication and policy making.

Real-time estimation of contact reduction enabled us to respond to urgent requests to actively inform rapidly changing public health policy amidst a pandemic. In early stages, the urgent need was to flatten the curve (Figure 4, panels A, B; Figure 5, panels A, B). Policymakers used initial projections to support decision making on the timing and scope of proposed social distancing policies and to compare potential healthcare need and existing capacity under different scenarios. Once infections began to decrease, there was interest in the degree of increased social contact that could be tolerated as the economy reopened without leading to overwhelmed hospitals (Figure 4, panels C, D; Figure 5, panels C, D). Model estimates were used to evaluate the impact of past policies and to forecast the impact of future proposed interventions, including permutations of layered policies or

Figure 5. Projected coronavirus disease ICU needs, Colorado, USA, 2020, if current trajectory continues (black line) and for a range of social distancing scenarios (colored lines) generated by using models calibrated at 4 time points during April–June (fit 1: Apr 3; fit 2: April 16; fit 3: May 15; fit 4: June 16). Current trajectory was based on estimated parameters generated for each fit. Social distancing is modeled as a percent reduction in the contact rate from baseline, and changes in social distancing are introduced 2 weeks after model fitting date. All other fitted parameters are held at the estimated values for each fit. Because ICU estimates from fit 1 were substantially higher than for later fits, the y-axis is scaled to 20,000 as opposed to 10,000 for fits 2–4. Colorado estimated ICU capacity (1,800 beds) is indicated by the dashed gray horizontal line. ICU, intensive care unit. Numbers in parentheses are current values.

Figure 6. Changes in population mobility before and after emergence of coronavirus disease, Colorado, USA, 2020, and comparison between mobility and estimated social distancing. A) Changes in mobility measured by the number hours spent away from home per day (source: SafeGraph, https://www.safegraph.com). Gray line indicates daily observations, and black line indicates a smoothed line using locally estimated scatterplot smoothing in R (https://www.r-project.org). The ribbon at the bottom indicates the 4 social distancing phases. B) Comparison between susceptible-exposed-infected-recovered model-estimated social distancing (colored boxes) and reduction in mobility relative to the preintervention period, January 29–February 15 (colored lines). Colors correspond to the 4 social distancing phases. Reductions in mobility are calculated as percentage decreases in time away from home relative to pre-epidemic baseline. C) Observed hospitalization data (red) and the simulated hospitalizations based on time away from home relative to a baseline mean during January 29–February 15. In the simulation, it is assumed there is no self-isolation of symptomatic infectious, no mask wearing, and no other transmission reduction to highlight the role of the mobility data in the simulation. P, phase.
interventions. Using locally derived estimates enabled policymakers to evaluate potential disease control strategies that were relevant to the current transmission trends in Colorado. For example, as the age distribution shifted within the epidemic in Colorado, estimates with contact rates that varied by age group were produced and used to evaluate policies or interventions targeted to specific age groups, such as return to school and alcohol last call policies.

A key challenge we faced was generating projections of hospital and critical care needs with limited data and rapidly evolving science. Early model estimates were imprecise because data were sparse and poor quality, leading projections to overestimate hospital needs. Estimates and, consequently, projections improved with greater data quantity and quality. Another challenge was the need to generate estimates under extreme time constraints. We designed a preliminary model in a matter of days and adapted it regularly to accommodate new data streams and science. The need for efficiency led to tradeoffs: for example, we did not account for age-specific contact rates (40). We present this material not as a finished work but to illustrate how models can be constructed and adapted in real time to inform critical policy questions.

The model findings were provided weekly to decision-makers in Colorado by written reports and briefings. These collaborative interactions provided an opportunity to review findings and define projection scenarios useful for decision-making. The rapidly developed, locally calibrated transmission model provided timely evidence of a moderate decrease in transmission in Colorado after an early transmission control policy began and a substantial decrease in the contact rate after stay-at-home orders that persisted after these policies were partially relaxed. Decreases in transmission mirrored changes in mobility through the end of stay-at-home, at which point mobility ceased to be a clear proxy for transmission. Locally calibrated models have local credibility and can be used to provide time-sensitive, tailored information to policymakers to assist their decision-making.

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References


Estimating the Impact of Statewide Policies to Reduce Spread of Severe Acute Respiratory Syndrome Coronavirus 2 in Real Time, Colorado, USA

Appendix

Case and Hospitalization Data

Two sources of data were used for model fitting. Initially, models were fit to reported cases which were obtained from the Colorado Electronic Disease Reporting System (CEDRS) because hospitalization data were not yet available. CEDRS is updated daily with cases of infection with severe acute respiratory syndrome coronavirus 2 (SARS-CoV-2) cases reported by private laboratories, public laboratories, hospital infection specialists, and state and local public health officials. CEDRS includes information regarding whether SARS-CoV-2 patients were hospitalized.

Starting in May, models were fit to daily SARS-CoV-2 hospital census data. These data were available daily in real-time from EMResource (https://emresource.juvare.com). The EMResource data appear to undercount hospitalizations in March compared with the reported hospitalizations among case-patients in CEDRS (Appendix Figure 1, top panel). On the basis of discussions with health officials and consistent with the literature, we inferred daily hospital census counts by using case data, assuming hospital length was an average of 8 days, starting with report date for hospitalized cases. Because of this discrepancy, we used inferred hospitalizations from the case data through April 7, and switched to EMResource daily hospital census data starting April 8.

Estimating the Start Date of the Epidemic

The first case of COVID19 reported in Colorado was reported on March 5, 2020, and had a reported symptom onset date of February 18, 2020. The next 3 reported cases had a symptom onset date of February 20, 2020. Assuming a 5.1-day incubation period (1,2), estimates that during the initial phase of the outbreak ≈85% of cases were unreported (3), and the outbreak has
a 5.2–6.4 day doubling time (4,5), we estimated the first cases occurred during January 17–29, 2020.

This estimate was derived by using the number of observed cases on a given day to estimate the number of true cases on the date of observation: \( n_t = n_o / u \), where \( u \) is the fraction of cases unobserved in early phases of the epidemic. We then used the estimated doubling time (T) to estimate the number of generations required to go from 1 case to \( n_t \) such that doubling time, \( G = \log_2(n_t) \). Because observed cases have an approximate exposure date equal to the onset date (\( D_o \)) minus the incubation period (I), we estimated the date of first introduction as \( D_o - I - T \). We estimated \( D_o \) separately for the 1 case that had an onset date of February 18 and the 3 cases that had an onset date of February 20, by using 5.2 and 6.4 as doubling times, yielding estimated date of first infection during January 17–29.

We note that this estimate is consistent with multiple evidence streams indicating introduction of SARS-CoV-2 in the Pacific Northwest in late January to early February (6,7). Such early introductions are plausible in Colorado, given the high degree of travel into the state during the winter ski season.

Model Details

We provide the model (Appendix Figure 2) and model equations. The model is age-structured and has 3 distinct age groups. The probability that a person becomes infected with SARS-CoV-2 is the same for all age groups. Once a susceptible person is infected, he or she moves to the exposed compartment in which they are not yet infectious. After spending time in the exposed compartment, a person can either be infectious and symptomatic or infectious and asymptomatic. We provide probabilities that an exposed person has symptoms and probabilities that a symptomatic person requires hospitalization that is age dependent (Appendix Table 1). Symptomatic persons are assumed to be infectious and presymptomatic for 1 of the 8 days they are infectious. On the basis of evidence suggesting that asymptomatic persons are less infectious than symptomatic persons (11), a parameter is included describing the ratio of infectiousness for symptomatic versus asymptomatic persons. We provide this parameter and other key model parameters (Appendix Table 2). It is assumed no further transmission occurs once the patient enters the hospital.
Model Equations

The susceptible-exposed-infected-recovered model describes the movement of the population of Colorado \((N)\) through the following model compartments: susceptible \((S)\), exposed \((E)\), infectious and symptomatic \((I)\), infectious and asymptomatic \((A)\) recovered \((R)\), hospitalized \((Ih)\), needing care in an intensive care unit (ICU) \((Ic)\), recovered from hospitalization or ICU \((Rh\ and\ \ Rc)\), and deaths \((D)\). The model is age stratified, such that there are compartments for each of the 3 age strata \((i)\) (<30, 30–59, ≥60 years). The subscripts indicate the age strata for each variable. For example, \(A_2\) is the number of asymptotically infected persons in the second age class (30–59 years). Similarly, \(\sum_{j=1}^{3}I_j\) is the sum of infected persons across the 3 age classes. Mask wearing \((mask_t)\), self-isolation of infectious persons \((sil_t)\) and social distancing \((SD_t)\) metrics are assumed to change over time, as indicated by the subscript.

\[
\frac{dS_i}{dt} = -\frac{\beta}{N} * \lambda * (1 - mask_t * 0.03) * (1 - sil_t) * (1 - SD_t) * S_i * \sum_{j=1}^{3} I_j - \frac{\beta}{N} * (1 - mask_t * 0.27) * (1 - SD_t) * S_i * \sum_{j=1}^{3} A_j
\]

\[
\frac{dE_i}{dt} = \frac{\beta}{N} * \lambda * (1 - mask_t * 0.03) * (1 - sil_t) * (1 - SD_t) * S_i * \sum_{j=1}^{3} I_j + \frac{\beta}{N} * (1 - mask_t * 0.27) * (1 - SD_t) * S_i * \sum_{j=1}^{3} A_j - \frac{1}{\alpha} * E_i
\]

\[
\frac{dI_i}{dt} = \frac{PS_i}{\alpha} * E_i - \frac{I_i}{\gamma}
\]

\[
\frac{dIh_i}{dt} = \frac{l_i}{\gamma} * hosp_i - \frac{1}{losh}
\]

\[
\frac{dIc_i}{dt} = \frac{l_i}{\gamma} * cc_i - \frac{1}{losc}
\]

\[
\frac{dA_i}{dt} = \frac{(1 - PS_i)}{\alpha} * E_i - \frac{A_i}{\gamma}
\]

\[
\frac{dR_i}{dt} = \frac{A_i + I_i(1 - hosp_i - cc_i)}{\gamma}
\]
\[
\frac{dR_{ih}}{dt} = \frac{lh_{i}}{losh}
\]
\[
\frac{dR_{ci}}{dt} = \frac{(1-d) \times I_{c_i}}{losc}
\]
\[
\frac{dD_{i}}{dt} = \frac{d \times I_{c_i}}{losc}
\]

The effective reproductive number \(R_e\) was estimated by using the following equation:

\[
R_e = \frac{\sum_{j=1}^{3} E_{j, t}}{\alpha} = \frac{\sum_{j=1}^{3} I_{j, t-a-1}}{Y}
\]

**Model Identifiability**

Analysis was performed using the computation in Omlin et al. (13). In this study, we have fit a social distancing parameter that switches at 4 different timepoints in the course of the hospitalization time series. A natural question is whether or not these 4 parameters are identifiable given the data. In Omlin et al. (13), the authors describe a colinearity index (gamma), which measures how the change in 1 parameter can be compensated by the fraction \(1 - 1/\text{gamma}\) change in other parameters. The gamma threshold for identifiability is conventionally set in the range of 10 to 15 (for gamma = 10, \(1 - 1/\text{gamma} = 90\%\)). We considered all possible combinations of 1, 2, 3, and 4 social distancing parameters and show the threshold (Appendix Figure 3). There is no issue with identifiability when trying to estimate \(\leq 3\) parameters. The collinearity of identifying all 4 parameters is \(\approx 10\), which is right on the edge of acceptability. In practice, we have not found this to be a problem because when we consider more recent hospitalization data, the previously estimated social distancing estimates do not change appreciably.

**Data and Code**

Model code, parameters, and data used to inform the fitting process can be found at https://github.com/agb85/CFpaper
References


Appendix Table 1. Estimated probability that an exposed (and latently infected) individual will be symptomatic, and a symptomatic individual will need hospital care*

<table>
<thead>
<tr>
<th>Age group, years</th>
<th>Probability of symptoms, given infection</th>
<th>Probability of non-ICU hospitalization given symptomatic COVID-19</th>
<th>Probability of needing ICU care given symptomatic COVID-19</th>
</tr>
</thead>
<tbody>
<tr>
<td>Colorado specific†</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>&lt;30</td>
<td>NA</td>
<td>0.00419</td>
<td>0.004</td>
</tr>
<tr>
<td>30–59</td>
<td>NA</td>
<td>0.056</td>
<td>0.019</td>
</tr>
<tr>
<td>&gt;60</td>
<td>NA</td>
<td>0.089</td>
<td>0.035</td>
</tr>
<tr>
<td>From the literature‡</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>&lt;30</td>
<td>0.18</td>
<td>0.006</td>
<td>0.0003</td>
</tr>
<tr>
<td>30–59</td>
<td>0.47</td>
<td>0.059</td>
<td>0.0045</td>
</tr>
<tr>
<td>&gt;60</td>
<td>0.79</td>
<td>0.207</td>
<td>0.0808</td>
</tr>
</tbody>
</table>

*The probability that an exposed person becomes symptomatic is based on the literature and adjusted to the age structure of the Colorado population. The probability a symptomatic person requires hospital care is based on Colorado case and hospitalization data and compared with estimates obtained from the literature. COVID-19, coronavirus disease; ICU, intensive care unit.

†The Colorado estimates were based on 2-part optimization by using Colorado hospitalization data and our age-structured susceptible-exposed-infected-recovered model. Colorado-specific estimates were only possible to derive with sufficient data starting in May and were incorporated into the model from then onwards (fits 3 and 4) in place of the literature-derived estimates.

‡Age-dependent probabilities that an infected person is symptomatic are based on estimates of Davies et al. (8). Age-dependent probabilities of hospitalization and ICU need are based on estimates summarized by (9). Because the age compartments of published estimates do not precisely align with our age categories, these estimates are a weighted sum of the age-specific probability of symptoms and the proportion of the population of Colorado within each age-compartment. Colorado demographic data of estimated population distribution in 2020 were based on US census projections. Literature-derived estimates of age-specific hospitalization and ICU need were used for fit 1 and fit 2. Literature-derived age-specific symptomatic fraction was used for all fitting.
### Appendix Table 2. Parameters in model and value estimates and sources*

<table>
<thead>
<tr>
<th>Symbol</th>
<th>Description</th>
<th>Estimate</th>
<th>Source</th>
</tr>
</thead>
<tbody>
<tr>
<td>$\beta$</td>
<td>Transmission rate: equivalent to combination of transmission probability and contact rate</td>
<td>Estimated from model</td>
<td>Model</td>
</tr>
<tr>
<td>$\lambda$</td>
<td>Ratio of infectiousness for symptomatic vs. asymptomatic persons. Evidence suggests that asymptomatic persons are less infectious than symptomatic persons (10). However, the comparative infectiousness is unknown.</td>
<td>Estimated from model</td>
<td>Model</td>
</tr>
<tr>
<td>$\gamma$</td>
<td>Incubation period</td>
<td>5.1 d</td>
<td>(1,10)</td>
</tr>
<tr>
<td>$\psi_S$</td>
<td>Age-specific probability of development of symptoms if infected</td>
<td>0.18 (age 0–29 years), 0.47 (age 30–59 years), 0.79 (age ≥60 years)</td>
<td>(8)</td>
</tr>
<tr>
<td>$\rho_I$</td>
<td>Probability symptomatic cases are identified by state surveillance</td>
<td>Estimated from model</td>
<td>Model</td>
</tr>
<tr>
<td>$\nu$</td>
<td>Age-specific probability of non-ICU hospitalization, given symptomatic infection</td>
<td>Appendix Table 1</td>
<td>NA</td>
</tr>
<tr>
<td>$\lambda_{sh}$</td>
<td>Non-ICU hospitalization length of stay</td>
<td>8 d</td>
<td>(9)</td>
</tr>
<tr>
<td>$\psi_C$</td>
<td>Age-specific probability of ICU-hospitalization, given symptomatic infection</td>
<td>Appendix Table 1</td>
<td>NA</td>
</tr>
<tr>
<td>$\lambda_{sc}$</td>
<td>ICU hospitalization length of stay</td>
<td>10 d</td>
<td>(9)</td>
</tr>
<tr>
<td>$\psi$</td>
<td>Probability of death, given ICU hospitalization</td>
<td>0.5</td>
<td>(9)</td>
</tr>
<tr>
<td>$N$</td>
<td>Total population</td>
<td>5,840,795</td>
<td>CDPHE</td>
</tr>
</tbody>
</table>

*CDPHE, Colorado Department of Public Health and Environment; ICU, intensive care unit. NA, not applicable
Appendix Figure 1. Top: daily number of hospitalized coronavirus disease patients based on Colorado Department of Public Health and Environment (blue lines) and EMResource (https://emresource.juvare.com) hospital census data (red lines). Middle: Severe acute respiratory syndrome coronavirus 2 cases reported to the state health department (Colorado Department of Public Health and Environment) by report date. Bottom: reported number of severe acute respiratory syndrome coronavirus 2 tests performed per day in Colorado.
Appendix Figure 2. Structure of the age-structured susceptible-exposed-infected-recovered model. Model includes separate compartments for the 3 age groups: 0–29 years, 30–59 years, and ≥60 years. ICU, intensive care unit.
Appendix Figure 3. Collinearity plot from identifiability analysis. In this study, we have fit a social distancing parameter that switches at 4 different timepoints in the course of the hospitalization time series.